

Database Management Systems

Relational Data Model

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A relational view of data

We can define a *relation* within the data from the mathematical perspective. Given the sets $X_1, X_2, \dots, X_n$ (not necessarily distinct), R is a relation on these n sets if it is a set of n -tuples each of which has its first element from X_1 , its second element from X_2 , and so on. We often refer to X_i as the i th attribute (taking values from a domain) of R .

As defined above, R is said to have degree n . Relations of degree 1 are often called unary, degree 2 binary, degree 3 ternary, and degree n n -ary.

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Note: There is no practical importance of defining a relation with degree 0.

Preliminaries

Example of a relation of degree 4:

Table: OSCAR

Year	Category	Movie	Name
1982	Best Costume Design	Gandhi	Bhanu Athaiya
1992	Lifetime Achievement Award	null	Satyajit Ray
2008	Best Original Song	Slumdog Millionaire	Gulzar
2008	Best Original Song	Slumdog Millionaire	A.R. Rahman
2008	Best Original Score	Slumdog Millionaire	A.R. Rahman
2008	Best Sound Mixing	Slumdog Millionaire	Resul Pookutty

The basic notions

In the Entity-Relationship (E-R) data model, we deal with multiple relations present in the data.

The E-R data model uses three basic notions as listed below:

- Entity sets
- Attributes
- Relationship sets

The basic notions

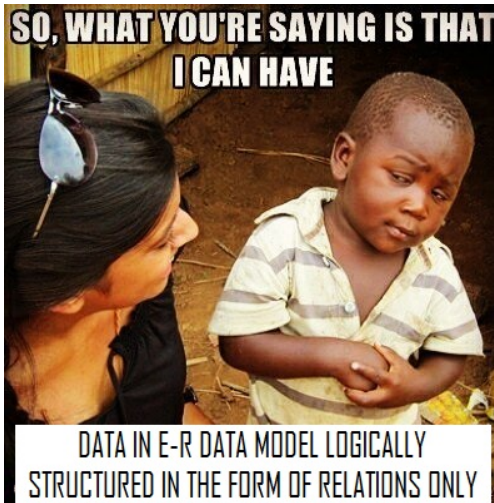
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Note: The Entity-Relationship (E-R) data model defines relations between the relations (tables).

The relations



Entity sets

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Note: Entity sets are not necessarily disjoint.

Entity sets

An entity signifies something that exists in real-world. It is like an object that is distinguishable from others. An entity is either *tangible* (exists physically) or *intangible* (exists only logically and have no physical existence).

Table: Musicians → Entity Type

Name	Aadhaar
Zakir Hussain	??????????????
Pt. Shiv Kumar Sharma	XXXXXXXXXXXXXX
Shivmani	*****
A. R. Rahman	@@@@@@@@@@@@@@

→ Entity 1

→ Entity 2

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Entity Set
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Attributes

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An attribute can be of different types as given below.

- Simple attribute – indivisible (e.g., age)
- Composite attribute – divisible (e.g., STD code and local code in a phone number)
- Single-valued attribute – takes a single value (e.g., gender)
- Multivalued attribute – takes multiple values (e.g., playing instruments)
- Derived attribute – value can be derived from other attributes (e.g., age can be derived from DOB)
- Descriptive attribute - takes descriptive value (e.g., reason of breaking a contract)

Let us brainstorm!!!

Relational data models are so powerful that it can represent any kind of real-life database scenarios, which bear relations therein. Imagine about a real-world environment where an attribute is considered as composite, multi-valued, and also derived in the same relational data model. Cite such an example.

Let us brainstorm!!!

Let there be a relation with the attribute `PerformerDOB`, a multi-valued attribute representing the date of births of active performers in a theatre group. It is also a composite attribute as one can derive the simple attributes like date, month and year of births from this. It is derived from `PerformerAge`, another attribute in the same relation having exact ages (in years, months and days) as entries.

Relationship sets

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Consider the following two entity sets 'Musicians' and 'Instruments'. We can define a relationship set 'Plays' to denote the association between musicians and the instruments they play.

Table: Musicians

Name	Aadhaar
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Table: Instruments

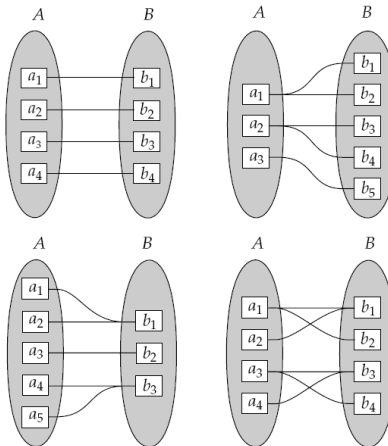
ID	Name	Key
1	Flute	G-Flat
2	Flute	B
3	Flute	B-flat
4	Guitar	E-flat

Constraints in E-R data model

An E-R data model may include the following types of constraints:

- Constraints on mapping cardinalities (also termed as constraints on cardinality ratios) – reflects the number of entities to which another entity can be associated via a relationship set
- Participation constraints – reflects the fraction of entities that can participate in at least one relationship
- Complex constraints – hybrid of other constraints
- Key related constraints

Constraints on mapping cardinalities



Constraints on mapping cardinalities

- One-to-one: An entity in A is associated with at most one entity in B , and an entity in B is associated with at most one entity in A .
- One-to-many: An entity in A is associated with any number (zero or more) of entities in B . An entity in B , however, can be associated with at most one entity in A .
- Many-to-one: An entity in A is associated with at most one entity in B . An entity in B , however, can be associated with any number (zero or more) of entities in A .
- Many-to-many: An entity in A is associated with any number (zero or more) of entities in B , and an entity in B is associated with any number (zero or more) of entities in A .

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- Many-to-many: An entity in A is associated with any number (zero or more) of entities in B , and an entity in B is associated with any number (zero or more) of entities in A .

As for example, the relationship set 'Plays' between the entity sets 'Musicians' and 'Instruments' is many-to-many.

Participation constraints

- Total participation: The participation of an entity set E in a relationship set R is said to be *total* if every entity in E participates in at least one relationship in R .
- Partial participation: The participation of an entity set E in a relationship set R is said to be *partial* if only some entities in E participate in at least one relationship in R .

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As for example, consider that an entity set 'Album' is associated with another entity set 'Musicians' via a relationship set 'Directs'. Then, the participation of 'Album' in the relationship set 'Directs' is total but the participation of 'Musicians' is partial.

Note: The constraints on mapping cardinalities are between the pairs of entity sets but the participation constraints are between an entity set and a relationship set.

Complex constraints

E-R diagrams can also reflect more complex constraints on the number of times each entity participates in relationships in a relationship set.

An edge between an entity set and a binary relationship set can be labelled with minimum and maximum cardinalities, shown in the form $l..h$. Here, $l \in \{0, 1, \dots, *\}$ and $h \in \{1, 2, \dots, *\}$ ($l \leq h$) denote the minimum and maximum cardinality, respectively.

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- A minimum value of 1 (i.e., $l = 1$) indicates total participation of the entity set in the relationship set.
- A maximum value of 1 (i.e., $h = 1$) indicates that the entity participates in at most one relationship, while a maximum value $*$ indicates no limit.

Note: A label $1..*$ on an edge is equivalent to a double line.

Concept of keys

A subset K of R is a *superkey* of R if, in any legal relation $r(R)$, for all pairs t_1 and t_2 of tuples in r such that $t_1 \neq t_2$, then $t_1[K] \neq t_2[K]$, i.e. no two tuples in any legal relation $r(R)$ may have the same value on attribute set K .

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An attribute of a relation R_1 is its *foreign key*, referencing another relation R_2 , if it is a *primary key* for R_2 .

Primary keys – A caution



Concept of keys

Table: OSCAR_DIRECTOR

Best Director	Awards	Nominations
John Ford	4	5
William Wyler	3	12
Frank Capra	3	6
Billy Wilder	2	8
David Lean	2	7
Fred Zinnemann	2	7
Steven Spielberg	2	7

In the above relational schema, {Best Director}, {Best Director, Awards}, {Best Director, Nominations} and {Best Director, Awards, Nominations} are all *superkeys* and {Best Director} is the only *candidate key*.

How to choose the primary key?

Although there is no Golden rule, many suggestions on choosing the primary key (from candidate keys) are available in practice.

- 1 The candidate key having attributes with no embedded spaces, special characters, or differential capitalization is better.
- 2 The candidate key having the least cardinality is better.
- 3 The candidate key having numeric (preferably integer) attributes is better.
- 4 The candidate key which is minimally updated is better.
- 5 The candidate key which is present in another table is better.
- 6 The candidate key having attributes that allow null values is not suitable.
- 7 The candidate key which is of derived type is not suitable.

Concept of keys

Table: SCORE

A	B	C	D	E	F
4	5	2	3	2	5
5	4	2	4	2	5
4	7	3	4	2	5
6	7	2	3	4	5

In the above relational schema, $\{A, B\}$ and $\{C, D, E\}$ are both *candidate keys*.

Concept of keys

Table: SCORE

A	B	C	D	E	F
4	5	2	3	2	5
5	4	2	4	2	5
4	7	3	4	2	5
6	7	2	3	4	5

In the above relational schema, $\{A, B\}$ and $\{C, D, E\}$ are both *candidate keys*. Let us assume $\{A, B\}$ is chosen as the primary key in SCORE. Then $\{A, B\}$ is a foreign key in relation RANK.

Table: RANK

R	A	B
1	4	5
2	5	4
3	4	7
4	4	5

Alternate key and Surrogate key

Candidate keys that are not chosen as the primary key are often termed as **alternate keys**.

We often use an additional surrogate key as the primary key. This could be an attribute like **ID** that takes auto-incremented values.

Weak and strong entity sets

If an entity set does not have sufficient attributes to form a primary key then it is termed as a *weak entity set*, otherwise it is termed as a *strong entity set*.

Special features – Specialization

An entity set may include subgroupings of entities that are distinct in some way from other entities in the set.

For instance, a subset of entities within an entity set may have attributes that are not shared by all the entities in the entity set. The E-R model provides a means for representing these distinctive entity groupings.

Special features – Generalization

There might exist similarities between two entities in the sense that they have several attributes in common. This commonality can be expressed by generalization, which is a containment relationship that exists between a higher-level entity set and one or more lower-level entity sets.

Higher- and lower-level entity sets also may be designated by the terms superclass and subclass, respectively.

Special features – Generalization

The *total generalization* demands that every entity in the superclass must belong to some subclass.

The *partial generalization* ensures that the entities in the superclass may not belong to any subclass.

The *disjoint generalization* demands that every subclass must be disjoint.

The *overlapping generalization* ensures that the same entity may belong to more than one subclass within a single generalization.

Special features – Attribute inheritance

A crucial property of the higher- and lower-level entities created by specialization and generalization is attribute inheritance. The attributes of the higher-level entity sets are said to be inherited by the lower-level entity sets.

Disadvantages

The limitations of entity-relationship data model are as follows:

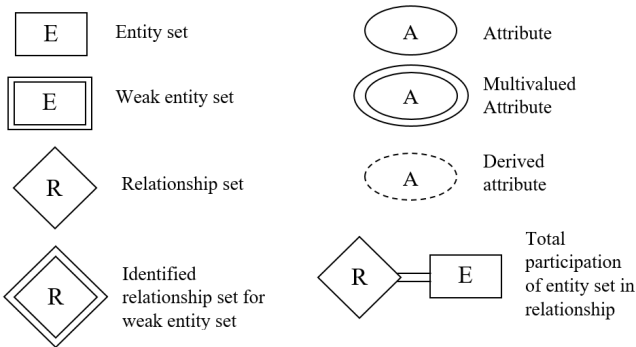
- **Hardware overheads:** It hides the implementation complexities and the physical data storage details from the users, thereby increasing the overhead on the hardware.
- **Ease of design:** As it is easy to design and use, it may lead to bad design.
- **'Information island' phenomenon:** It creates a situation where too many people will come up with their own databases and applications.

The components in Entity-Relation (E-R) diagram

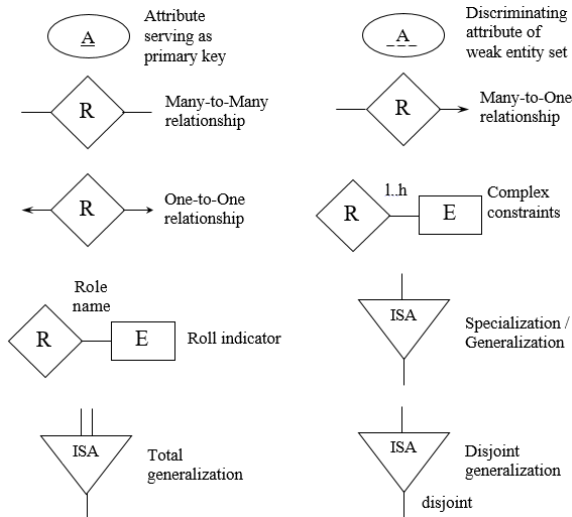
An E-R diagram graphically represents the entire logical structure of a database. It comprises the following components.

- Rectangles
- Double rectangles
- Diamonds
- Double diamonds
- Ellipses
- Double ellipses
- Dashed ellipses
- Lines
- Double lines
- and so on

The components in Entity-Relationship (E-R) diagram

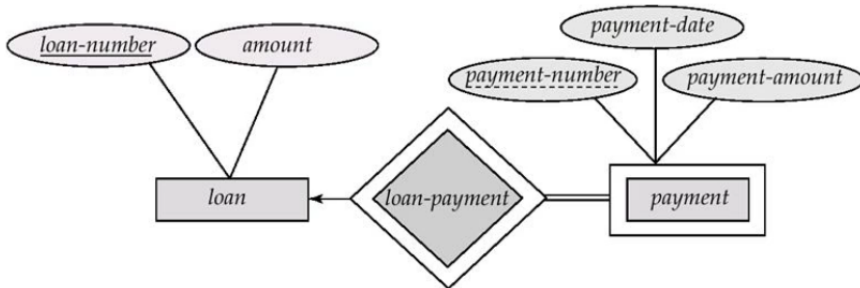


The components in Entity-Relationship (E-R) diagram



Discriminating attribute of weak entity set

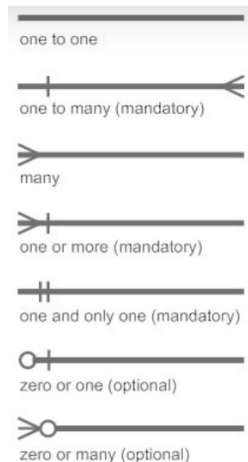
A primary key does not exist for a weak entity set. However, it contains a partial key termed as *discriminating attribute* that can identify a group of entities from the entity set.



The combination of *discriminating attribute* and primary key of the strong entity set makes it possible to uniquely identify all entities of the weak entity set.

Mapping cardinality constraints – Style 1

Crow's Foot / Information Engineering Notation:



Mapping cardinality constraints – Style 2

Chen Notation:



$1:N$ ($n=0,1,2,3\dots$)
one to zero or more

$M:N$ (m and $n=0,1,2,3\dots$)
zero or more to zero or more
(many to many)

$1:1$
one to one

Mapping cardinality constraints – Style 3

Bachman Notation:



one to one



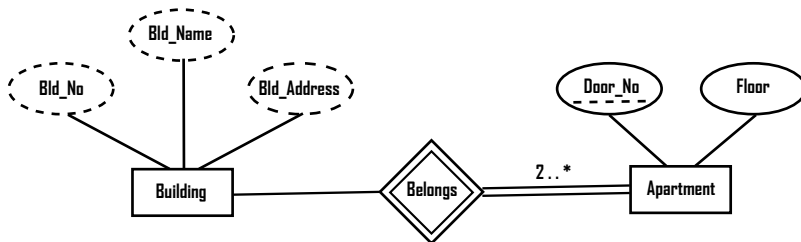
zero or more to one or more



one to one or more

Let us brainstorm!!!

Consider the following E-R diagram. It represents the details about real-estate properties of a company. The diagram has been prepared by a novice developer without much understanding of Relational Data Model. Can you list up the inconsistencies present in the diagram?



Let us brainstorm!!!

Here follow the problems in the given E-R diagram:

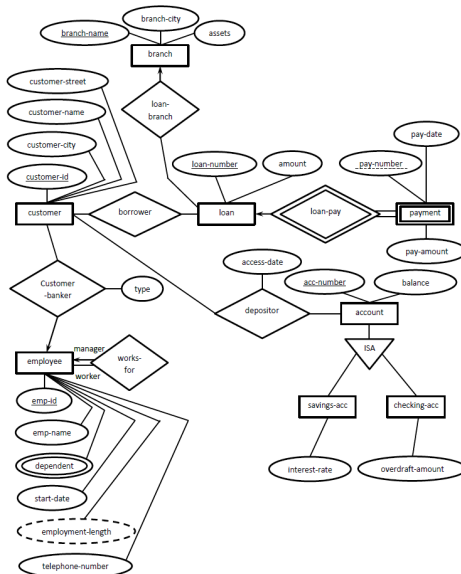
- (i) All the attributes of the entity set Building cannot be of derived type (shown with dashed ellipses). There is no other attribute from which they will be derived.
- (ii) If Belongs is weak relation (shown with double diamond), either of the Building or Apartment has to be a weak entity set (shown with double rectangle).
- (iii) The mapping cardinality constraints (shown with 2..*) and participation constraints (shown with double line) are conflicting for the entity set Apartment. If the minimum cardinality constraint is 2 it cannot be a total participation.
- (iv) If there is a discriminating attribute (shown with dashed underline) for the entity set Apartment, then there has to be a set of attributes that can serve as the primary key (shown with underline) for the related entity set Building.

Entity-Relation (E-R) diagram – Specialization and generalization

In E-R diagrams, specialization (and also generalization) is depicted by a triangle component labeled ISA (standing for “is a”) which denotes that an entity (say a musician) “is a” part of another entity (say a person).

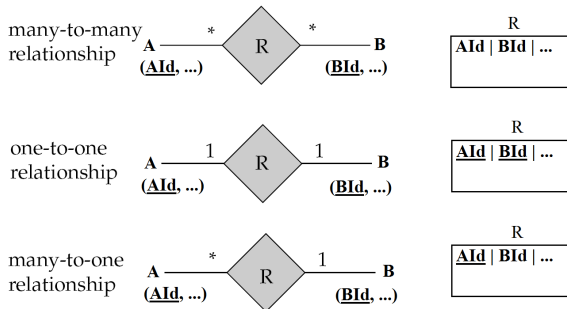
The ISA relationship may also be referred to as a superclass-subclass relationship. Higher- and lower-level entity sets are depicted as regular entity sets—that is, as rectangles containing the name of the entity set.

The E-R diagram for a banking system



Converting an E-R diagram to relations

The mapping cardinality constraints help to identify the primary keys in the relations constructed from the relationship sets.



Converting an E-R diagram to relations

```
branch(branch-name, branch-city, assets)
customer(customer-id, customer-name, customer-street,
customer-city)
loan(loan-number, amount)
payment(pay-number, pay-date, pay-amount)
employee(emp-id, emp-name, dependent, employment-length,
start-date, telephone-number)
account(acc-number, balance)
savings-acc(acc-number, balance, interest-rate)
checking-acc(acc-number, balance, overdraft-amount)
loan-branch(loan-number, branch-name)
borrower(customer-id, loan-number)
loan-pay(loan-number, pay-number)
customer-banker(customer-id, emp-id, type)
depositor(customer-id, acc-number, access-date)
works-for(emp-id, emp-id)
```

The E-R diagram for Amazon Freedom Sale

The screenshot shows the Amazon India homepage during the Freedom Sale. The header includes the Amazon.in logo, a search bar, and navigation links for account, orders, and Prime. The main banner features a large 'FREEDOM SALE' badge for August 8th to 11th, with the text 'Start shopping'. Below the banner, there are four promotional tiles: SBI card 10% Instant Discount, NO COST EMI on 10 crore+ products, FREE DELIVERY on first order, and EXCHANGE OFFER. The bottom section is titled 'Blockbuster Deals' with filters for 'All Available', 'Upcoming', and 'Missed'.

amazon.in
Try Prime

All ▾

Hello. Sign in
Account & Lists ▾

Orders

Try Prime ▾

0 Cart

Deliver to
Andharmanik 743503

Shop by
Category ▾

Your Amazon.in

Today's Deals

Freedom Sale | Live now

FREEDOM SALE
8TH - 11TH AUG

Start shopping

SBI card
10% Instant Discount*
with SBI Credit Cards
*Also with Credit Card EMI | T&C apply

NO COST EMI
on 10 crore+ products
Debit/Credit cards | **BAJAJ FINSERV**

FREE DELIVERY
on first order*
*T&C apply

EXCHANGE OFFER
Up to *6,000 off* on exchange
*T&C apply

Blockbuster Deals

All Available Upcoming Missed

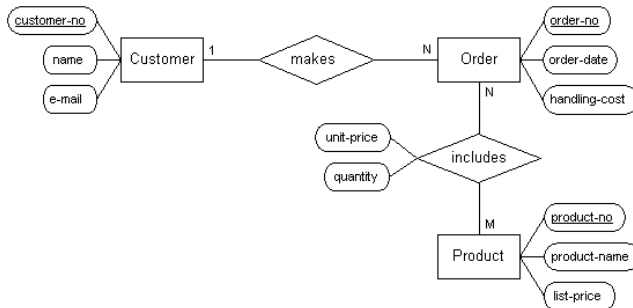
Category ▾

The E-R diagram for Amazon Freedom Sale

Amazon is celebrating the 74th Independence Day of India through Freedom Sale during August 8-11, 2020. Amazon plans to store the details about their products, customers, and the orders that are placed by the customers in a relational database. Prepare an E-R diagram based on the following requirements.

- 1 Each product has a unique identifier, a name, and a listed price.
- 2 Each customer has a unique identifier, a name, and an e-mail ID.
- 3 Every order placed under the Freedom Sale includes a unique identifier, a date, and a handling cost.
- 4 There is a unit price and quantity associated with each order for a particular product.

The E-R diagram for Amazon Freedom Sale



The E-R diagram for a polyclinic

Suppose a polyclinic wishes to store the information about their doctor and patient details in a database. Prepare an E-R diagram considering the following features.

- 1 Each doctor having chamber in the polyclinic has a unique ID, a first name and a last name.
- 2 Each patient attending the polyclinic has a unique ID, a first name, a last name, and a insurance number (not necessarily unique).
- 3 Each doctor has specialization (one or more) with ID and descriptions. However, no two doctors can have the same set of specializations.
- 4 Each patient has diagnosis details (one or more) with a unique code.
- 5 A doctor can attend multiple patients and a patient can visit multiple doctors.

The E-R diagram for a polyclinic

